

Con. 6624-10.

(REVISED COURSE)

GT-7590

(3 Hours)

[ Total Marks : 100

- N.B. : (1) Question No. 1 is **compulsory**.  
 (2) Attempt any **four** questions out of remaining **six** questions.  
 (3) Assume **suitable** data if **required**.

1. (a) Check whether the following system is linear, stable and time invariant or not. 6  
 (i)  $y(n) = ne^{x(n)}$   
 (ii)  $y(n) = 4x(n+2) + 5$   
 (iii)  $y(n) = 8 \cos \omega_0 n x(n)$ .

- (b) State and prove convolution property of Z-transform. 5  
 (c) Explain Parseval's energy relationship. 5  
 (d) Find the linear convolution of two sequences given by :- 4

$$x(n) = [1, 2, 3, 4]$$

$$h(n) = [4, 1, 2, 1]$$

2. (a) Obtain cascade and parallel realization for the following IIR filter :- 10

$$H(z) = \frac{8z^3 - 4z^2 + 11z - 2}{(z - 0.25)(z^2 - z + 0.2)}$$

- (b) A second order recursive system is described by :- 10

$$y(n) = \frac{1}{4} u(n-1) - \frac{1}{8} y(n-2) + x(n) - x(n-1)$$

(i) Find the unit sample response

(ii) Find the response to input  $x[n] = (\frac{1}{2})^n u(n)$  with zero initial condition.

3. (a) Using DIF FFT, find DFT of following sequence :- 10

$$x(n) = \{1, 2, 3, 4, 1, 2, 3, 4\}$$

- (b) Using results in Q.3 (a) Find  $X_2(k)$  if  $x_2(n) = x(n-2)$ . 5

- (c) Using results in Q.3 (a), Find  $X_3(k)$  if  $x_3(n) = x^*(n)$ . 5

4. (a) Design a digital Butterworth low pass filter satisfying the following specifications 10  
 using bilinear transformation (Assume  $T = 1s$ )

$$0.9 \leq |H(e^{j\omega})| \leq 1; 0 \leq \omega \leq \frac{\pi}{2}$$

$$|H(e^{j\omega})| \leq 0.2; \frac{3\pi}{4} \leq \omega \leq \pi$$

- (b) Determine the filter co-efficients  $h(n)$  for the desired frequency response of a low pass filter. 10

$$H_d(e^{j\omega}) = \begin{cases} e^{-j2\omega}; & -\frac{\pi}{4} \leq \omega \leq \frac{\pi}{4} \\ 0 & ; \frac{\pi}{4} \leq \omega \leq \pi \end{cases}$$

Using Hamming Window.

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Con. 6624-GT-7590-10.

2

5. (a) The difference equation of the system is given by :

$$y(n) = 3y(n-2) + 2y(n-1) + x(n)$$

and

$$x(n] = (1/2)^n u(n) \text{ with } y(-1) = y(-2) = 1.$$

Determine :

- (i) Zero input response
- (ii) Zero state response
- (iii) Total response.

12

- (b) Determine inverse Z-transform of  $x(z) = \frac{1}{1 - \frac{3}{2}z^{-1} + 0.5z^{-2}}$  for all possible ROC. 8

6. (a) With the help of block diagram, explain TMS 320 (5x series of processors). 10

- (b) Derive the radix-2 DIF-FFT for a 8-point DFT. 10

7. Write short notes on any four :- 20

- (a) Applications of DSP in biomedical field
- (b) Energy and Power Signals
- (c) Filtering of long data sequences
- (d) Relationship between Z-transform and Fourier transform
- (e) Adaptive noise cancellation.